

# Computational Geometry/Review

4/22/2009

# Opening Discussion

- Do you have any questions?
- Minute Essay comments
  - Review session in class
  - Why?
  - Banking stress test simulation.

# Computational Geometry

- Many different types of problems require handling geometry.
- When simulations are done with a spatial element they also include geometric elements.
- Computational geometry is the study of efficient and correct algorithms for dealing with geometry.

# Convex Hull

- Our first example is finding the convex hull of a set of points. This is the smallest convex polygon that contains all the points.
- A shape is convex if given any two points,  $a$  and  $b$ , in the shape, all the points on segment  $ab$  are also in the shape.

# First Algorithm

- Run through all pairs of points
  - For each pair if all other points are to the right of the directed line, add that segment to a list.
- Link up the segments that you find in the end.
- This has several problems. It isn't robust with floating point numbers. It needs to be adjusted for degeneracies. It is  $O(n^3)$ .

# Improved Algorithm

- Sort the points by x and add first two to a list.
- Run through remaining point and
  - Append next point to list
  - While the list has more than two points and the last three don't make a right turn
    - Delete the middle of the last three.
- Repeat this process in reverse order to make lower hull.
- Append lower and upper.
- Runs in  $O(n \log n)$  time.

# Spatial Partitioning

- When we talked about collisions we talked about using a grid to partition the space so that we could find collisions efficiently.
- Grids are fast, but they are not very flexible. Trees are much more flexible.
- The 1-D example of a tree is something you will find familiar.
- Data can go in all nodes or just leaves.

# Fast Gravity Calculations

- One use of spatial partitioning in simulation has been efficient approximations to gravitational forces.
- Like collisions, a standard gravity algorithm requires  $O(n^2)$  work. Unlike collisions, gravity is long range so you can't just search nearby.
- Long range forces can be approximated by grouping particles. Spatial trees are the standard method of doing this.



# Review

- For the rest of the class time we will talk about the second exam.
- We can schedule a review session for Thursday afternoon as well if you would like.

# Minute Essay

- Do you have any questions?
- The second test is on Friday.