

No Data/Poisson Processes

2/25/2011

Opening Discussion

- What did we talk about last class?

Dealing with Insufficient Data

- Ask SMEs for what they think the bounds and the mean should be.
- Use triangle distribution to match those numbers.
- Find beta distribution that gives you the right shape.

Poisson Processes

- Arrivals are often well modeled by a Poisson process.
- A Poisson process is defined as having three characteristics.
 - Events happen one at a time.
 - The number of events between t and $t+s$ is independent of the number of earlier events.
 - The number of events between t and $t+s$ is independent of t .

Properties

- If $N(t)$ is a Poisson process then the following is true.

$$P[N(t+s) - N(t) = k] = \frac{e^{-\lambda s} (\lambda s)^k}{k!}$$

- For $k=0,1,2,\dots$ and $t,s \geq 0$
- If $N(t)$ is a Poisson process with rate of λ then the interarrival times, A_1, A_2, \dots are IID exponentials with mean of $1/\lambda$.

Nonstationary Poisson Process

- Throw out the third requirement.
- Let $\Lambda(t) = E[N(t)]$.

$$\lambda(t) = \frac{d}{dt} \Lambda(t)$$

- Then

$$P[N(t+s) - N(t) = k] = \frac{e^{-b(t,s)} [b(t,s)]^k}{k!}$$

$$b(t,s) = \Lambda(t+s) - \Lambda(t) = \int_t^{t+s} \lambda(y) dy$$

Related Tangent

- This discussion in the book was actually quite enlightening for an article I read in *Physics Today* recently.
- The article was about light emission from nanoprocesses.
- The distribution of illumination for these is not a exponential. That implies it is not a Poisson process, and that means there is a more complex mechanism involved.

Power-law Distribution

- The distribution of on and off times followed a power-law distribution. This is also a common distribution in many other areas, including planetary science.
- Both differential and cumulative distributions have the same form of x^{-q} .
- Particle sizes like to follow this with a differential q of about 3.

Minute Essay

- The midterm is next class. Do you have any other suggestions for questions?
- Feel free to bring a single sheet of paper cheat sheet. I don't know if it will help but it is a good way to study.