

Magnitude | 0 0 0 Residue

$ y \leftrightarrow \%:y^*+y$. For example: $\begin{array}{r} 6 _6 3j4 \\ 6 6 5 \end{array}$	The familiar use of residue is in determining the remainder on dividing a non-negative integer by a positive: $\begin{array}{r} 3 0 1 2 3 4 5 6 7 \\ 0 1 2 0 1 2 0 1 \end{array}$
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The definition $y-x^* < . y \% x+0=x$ extends the residue to a zero left argument, and to negative and fractional arguments. For example:

```

over =: ({. ,.@; }.).@":@,
by   =: ' '&@;@,.@[ ,. ]
x=: 3 2 1 0 _1 _2 _3 [ y=: 0 1 2 3 4 5 6 7 8
x by y over x | / y
+---+
| |0 1 2 3 4 5 6 7 8|
+---+
| 3|0 1 2 0 1 2 0 1 2|
| 2|0 1 0 1 0 1 0 1 0|
| 1|0 0 0 0 0 0 0 0 0|
| 0|0 1 2 3 4 5 6 7 8|
|_1|0 0 0 0 0 0 0 0 0|
|_2|0 _1 0 _1 0 _1 0 _1 0|
|_3|0 _2 _1 0 _2 _1 0 _2 _1|
+---+

```

To produce a true zero for cases such as $(\%3) | (2\%3)$ the residue is made tolerant as shown in the definition of `res` below:

```

res=: f`g@.agenda"0
agenda=: ([ = 0:) +. (<. = >.)@S
S=: ] % [ + [ = 0:
f=: ] - [ * <.@S [ , g=: ] * [ = 0:
0.1 res 2.5 3.64 2 _1.6
0 0.04 0 0

```

Continued

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```
(. . i res/~ i |/~) a=: 2 -~ i.5
+-----+
|_2| 0 _1 0 _1 0 | 0 _1 0 _1 0 |
|_1| 0 0 0 0 0 | 0 0 0 0 0 |
| 0|_2 _1 0 1 2 |_2 _1 0 1 2 |
| 1| 0 0 0 0 0 | 0 0 0 0 0 |
| 2| 0 1 0 1 0 | 0 1 0 1 0 |
+-----+
```

The dyad | applies to complex numbers. Moreover, the fit conjunction may be applied to control the tolerance used. The dyad m&|^ on integer arguments is computed in a way that avoids large intermediate numbers. For example: 2 (1e6&|^) 10^100x