

Exponential ^ 0 0 0 Power

<p>x^y is equivalent to $e^{y \ln x}$, where e is Euler's number e^1 (approximately 2.71828). The natural logarithm (\ln) is inverse to e^{\cdot} (that is, $y = \ln e^y$ and $e^{\ln y} = y$).</p> <p>The monad $x \&^{\cdot}$ is inverse to the monad $x \&^{\cdot}$. For example:</p> <pre> 10&^ 10&^ . 1 2 3 4 5 1 2 3 4 5 10&^ . 10&^ 1 2 3 4 5 1 2 3 4 5 </pre>	<p>x^2 and x^3 and $x^{0.5}$ are the square, cube, and square root of x.</p> <p>In general, x^y is $e^{y \ln x}$, applying for complex numbers as well as real.</p> <p>For a non-negative integer y, the phrase $x \wedge y$ is equivalent to $x \text{ */ } y \# x$; in particular, */ on an empty list is 1, and $x \wedge 0$ is 1 for any x, including 0.</p> <p>The fit conjunction applies to \wedge to yield a stope defined as follows: $x! . k \ n$ is $x! / (x - k)!$. In particular, $\wedge! . _1$ is the falling factorial function.</p>
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The last result in the first example below illustrates the falling factorial function, formed by the fit conjunction. See Chapter 4 of [8] for the use of stope functions, stope polynomials, and Stirling numbers in the difference calculus:

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e=: ^ 1 [ x=: 4 [ y=: 0 1 2 3
, .&. > x (e"_ i e&^@] i ^ i ^@([ * ^.@]) ; ([^]) ; ^!._1) y
+-----+-----+-----+-----+-----+
| 2.71828 | 1 | 1 | . | 1 | 1 |
|          | 2.71828 | 4 | 1 | 1 | 4 |
|          | 7.38906 | 16 | 4 | 4 | 12 |
|          | 20.0855 | 64 | 27 | 27 | 24 |
+-----+-----+-----+-----+-----+

S2=: %.@S1=: (^!._1/~ % . ^/~) @ i. @ x:
(S1;S2) 8
+-----+-----+-----+-----+-----+
| 1 0 0 0 0 0 0 0 | 1 0 0 0 0 0 0 0 |
| 0 1 _1 2 _6 24 _120 720 | 0 1 1 1 1 1 1 1 |
| 0 0 1 _3 11 _50 274 _1764 | 0 0 1 3 7 15 31 63 |
| 0 0 0 1 _6 35 _225 1624 | 0 0 0 1 6 25 90 301 |
| 0 0 0 0 1 _10 85 _735 | 0 0 0 0 1 10 65 350 |
| 0 0 0 0 0 1 _15 175 | 0 0 0 0 0 1 15 140 |
| 0 0 0 0 0 0 1 _21 | 0 0 0 0 0 0 1 21 |
| 0 0 0 0 0 0 0 1 | 0 0 0 0 0 0 0 1 |
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$S1$ gives (signed) Stirling numbers of the first kind and $S2$ gives Stirling numbers of the second kind. They can be used to transform between ordinary and stope polynomials. Note that $x:$ gives extended precision.