







Binary Search Trees — Definitions

• Trees are a special type of "graph" (collection of nodes connected by edges), in which one node is called the root and has any number of outgoing edges but no incoming edges, and other nodes have one incoming edge and any number of outgoing edges. Each node can store some data.

Useful for representing hierarchies of various kinds (e.g., the files/directories in a file system).

- "Binary trees" are trees in which each node has at most two children.
- "Binary search trees" are binary trees where the data is something that can be ordered, and for each node, everything in its left subtree is "smaller" while everything in its right subtree is "larger". This makes them good for storing a sorted collection that needs to grow/shrink.

Binary Search Trees — Operations

 With all trees, various kinds of "traversal" (visit all nodes) are possible. For BSTs, "in-order" (left subtree, then root, then right subtree) gives you the data in sorted order (why?). Easy to describe recursively; without recursion pretty tricky.

- "Insert" is not too hard and can be described recursively: Inserting into an empty (sub)tree just means adding the thing to insert as the root node.
- "Find" is also not too bad and easy to describe recursively.
- "Remove" is significantly more difficult: Some cases are easy (removing a leaf), but the worst case, removing a node with two children, is tougher. What works is to replace the node to remove with either the largest element of its right subtree or the smallest element of its left subtree.

