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## Administrivia

- Reminder: Homework 10 due Monday.

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## Linked Lists in C, Continued

- In class Monday we talked about linked lists, and I showed the beginnings of code for a sorted linked list of `ints`.
- Look briefly at it again ... (We won't go into details in class, but it's on the "sample programs" page if you're curious.)

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### “Collections” Types Review/Revisited

- Can think of a “collection type” as a way of representing a collection of data items. Arrays are one; linked (linear) lists are another.
- There are many others, all beyond what we can cover in this course; more-advanced courses in programming and computer science are apt to discuss many or all of these . . .

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### Sidebar: Abstract Data Types

- In computer science we talk often about “abstract data types”.
- Somewhat formally, an abstract data type is a set of values and some operations on them.
- Simple example: fixed-size integers, with obvious(?) values and operations including arithmetic and bit manipulation.
- Simple example: Boolean values, also with obvious values and operations including logical “and”, logical “or”, etc.
- Less simple example: Linear list, with operations including insert, delete, traverse, indexed access. Could be implemented with an array or with a linked-list structure.

## Stacks

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- A “stack” is a list of values of a particular type (integers, say, or something more complicated), with a restricted set of operations, often just “enqueue” (add to the “tail” of the queue), “pop” (remove and return the top element), and “is empty?” (I.e, this is a “last-in, first-out” linear list.)
- Turns out to be widely useful. This idea is how functions (including recursive ones) are typically implemented, with a stack each element of which contain values passed to the function, local variables, and a “return address”.
- Could be implemented using an array or as linked list.

## Queues

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- A “queue” is a list of values of a particular type (integers, say, or something more complicated), with a restricted set of operations, often just “enqueue” (add to the “tail” of the queue), “dequeue” (remove and return the first element), and “is empty?” (I.e, this is a “first-in, first-out” linear list.)
- Also widely useful any time you need to maintain something in first-in first-out order.
- Could be implemented using an array (“circular queue” idea) or as linked list.

## Trees

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- A “tree” in computer science is a way of representing data organized in some hierarchical way. Each is a collection of “nodes” that store a value and pointers to “child nodes”.
- In the same way as a linked list is represented by a pointer to the first node, a tree is represented by a pointer to its “root node”.
- Useful any time you want to represent a hierarchical structure (directories and files, e.g.).

## Trees, Continued

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- “Binary trees” (in which each node has at most two children) are simpler to represent and effective in many situations.
- “Binary search tree” is a binary tree where everything in the “left subtree” of a node has smaller values and everything in the “right subtree”. Allows faster lookup, sort of like binary search in an array.
- “Heap” is a binary tree where everything in *both* subtrees of a node has larger values. Useful for maintaining a “priority queue” (with operations including “remove and return smallest element” and “insert element”).

## Graphs

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- In some mathematical contexts, “graph” means a collection of nodes and edges connecting them. Edges can be uni- or bi-directional. Nodes can store values, and associated with each edge there can also be a value (a “weight”).
- Also turns out to be widely useful as a way of representing all kinds of things — e.g., the classic traveling-salesperson problem.
- Can implement used a linked data structure or with various types of 2D arrays.

## Associative Array

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- An associative array is a way of storing (key, value) pairs. Conceptually it's an array of such pairs, with operations that would include insert, delete, and lookup (find the value associated with a key).
- Widely useful in situations where you want a collection of data with an easy way to find particular elements. (For example, in a program to compute student grades, you might have an associative array where the key is a student name and the value is that student's scores.)
- Provided by many higher-level languages (e.g., Scala has “maps”, and Python has “dictionaries”). In C it's more work but (of course?) doable.

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### Hash Table

- A “hash table” is a meant-to-be-efficient way of implementing an associative array, such that looking up a value using the key is reasonably fast.
- Basic idea is to define a reasonably-sized array and some way to map from a key to an index into this array (“hash function”). Each element of the array points to a list of (key, value) pairs, and to look for a particular key, you use the hash function to map into the array and then search the list.  
If the hash function and the table size are well-chosen, these lists will be short, perhaps in many cases of length 1, making lookup fast.
- Also widely useful in the many circumstances in which fast lookup is desirable. (As an example — in a minute essay last year someone asked about fast access to items in “a database”? this idea would probably work for that.)

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### “Ragged Arrays”

- (This isn’t really an abstract data type, but it’s another kind of collection, so mention it here.)
- Sometimes useful to be able to define a “ragged array” — an array in which rows can have different sizes. Not difficult in C, if you represent each row as an array and have some way of remembering sizes of rows.
- An obvious(?) example is the second argument to `main` — it’s a ragged array of characters, with no need to explicitly save how many columns in each row since strings are null-terminated.

### Minute Essay

- Can you think of situations in which one of these collection types (linear lists, trees, graphs, etc.) would be useful?
- There's so much we just haven't been able to cover in this course. Any questions you'd like me to try to answer Monday?

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