



Slide 2



Order of Magnitude of Functions, Continued

• How to determine an order of magnitude for functions?

If we look at graphs of functions, we might notice that we can classify them into groups based on their "shape".

For nondecreasing functions, we also notice that some shapes "grow" faster than others.

Examples?

· Idea is that we want functions that have the same shape to have the same order of magnitude.

Slide 4

Order of Magnitude of Functions, Continued

• Formal definition:

Write $f=\Theta(g)$ to mean that f and g have the same order magnitude. Define to be true iff there are positive constants $n_0,\,c_1,\,c_2$ such that for all $x\ge n_0$

$$c_1 g(x) \le f(x) \le c_2 g(x)$$

In other words, these functions are roughly proportional to each other.

- Try an example: f(x) = x 10, g(x) = 3x + 2.
- Of course this is incredibly tedious, so people have come up with (and proved) general rules for polynomials, other common functions.



Slide 5

Slide 7 Minute Essay • Which of the following functions are $O(N^2)$? $f(N) = 100N^2$ $g(N) = N^2 + N - 1000$ $h(N) = N^3$ • Which of the following functions are $O(2^N)$? $f(N) = 2^N - 5$ $g(N) = 10^N$ h(N) = N!