









Slide 5

Strengthening Preconditions, Weakening Postconditions (Review)

• If we have $\{Q\} P \{R\}$ then for "stronger" precondition Q_1 (i.e., $Q_1 \rightarrow Q$) we can derive $\{Q_1\} P \{R\}$ and for "weaker" postcondition R_1 (*i.e.*, $R \rightarrow R_1$) we can derive $\{Q\} P \{R_1\}$



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Examples of Less Formal Use

• Rule for sequential composition leads to "programming with assertions" — at "interesting" points in the program, use to document/check what you know to be true at that point. Example: Program that first sorts an array, then repeatedly performs binary search. Could use assertion to document that array is sorted.

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• Rule for conditionals can also be used informally: Code for "if" branch only has to work if condition is true; code for "else" branch only has to work if condition is false. Example: Function to compute root(s) of quadratic equation.

Semi-Intermezzo: A Puzzle

- Suppose you have a jar containing white marbles and black marbles, plus an unlimited supply of extra black marbles, and you do the following:
 - 1. Select two marbles.
 - 2. If they're the same color, discard them both and put a black marble in the jar. If they're different colors, discard the black one and put the white one back in the jar.
 - 3. If there are at least two marbles in the jar, repeat.
- Does this end? If it does, what if anything can you say about the marble(s) in the jar when it ends?
- (Similar ideas behind "metric" for loop termination and "invariant" for loop correctness.)







