

Slide 2

Sets (This will likely be review for most of you!) Definition: Informally, a set is a collection of objects (unordered, no duplicates). Formally — well, formal definitions are surprisingly difficult! Some notation — for x an object and A a set, x ∈ A means — ? y ∉ A means — ? We say two sets are equal exactly when they have the same members.



Subsets • $A \subseteq B$ exactly when every element of A is also in B. "Proper" subset is when $A \neq B$. For what sets S is the empty set a subset of S? • If $A \subseteq B$ and $B \subseteq A$, what do we know about A and B?

Slide 4



Slide 6

Operations on Sets Union: A ∪ B = {x | x ∈ A ∨ x ∈ B}. Intersection: A ∩ B = {x | x ∈ A ∧ x ∈ B}. What does "A and B are disjoint" mean? Complement: A' = {x | x ∈ S ∧ x ∉ A}, where S is some "universal set" (without which this definition doesn't make sense) — integers, people, etc. Difference: A - B = {x | x ∈ A ∧ x ∉ B}. Cartesian product: A × B = {(x, y) | x ∈ A ∧ y ∈ B}.



Countable and Uncountable Sets
If A and B are finite sets, fairly obvious what it means for them to be "the same size", right?
Is there some way to extend this to notion of "size" for infinite sets?









