





Proof Techniques, Continued

- Suppose you have a "conjecture" (e.g., "all odd numbers greater than 1 are prime"). How to (try to) prove it?
- Well, first must sometimes decide whether to prove it. Do you think it's true?
- If it's a statement about all integers, etc., often helpful to start with "inductive reasoning" — try some examples and see what happens.
- If one doesn't work? "Counterexample" that shows conjecture false.
- If all succeed? Just means you didn't find a counterexample. So, turn to "deductive reasoning" to prove — subject of first part of chapter 2.
- Lots of examples/problems will be simple stuff about integers. Why? Something where we supposedly all know the "context".











## Hinute Essay Find a counterexample for the following conjecture: "If *x* is an integer, √*x* is an integer." To show that there is no largest prime, we could assume *P* and derive a contradiction. What is *P*? (You don't have to show there's no largest prime, just say what *P* is.)

