## Administrivia

- About homeworks: Feedback on your work is coming. In the meantime, I will try to post sample solutions this week.
- About projects: If you haven't turned in a proposal yet, please do at your earliest convenience!


## Slide 1

## Minute Essays From Previous Lectures

- What people found interesting/difficult about Homework 3 (game of life):
- Message-passing!
- Lesson in basic program design / something that's easy in one paradigm is difficult in another.

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- What people found interesting/difficult about Homework 4 (quicksort):
- Knowing when the sort was finished.
- Getting data to the new thread (?).
- How quicksort works.
- The importance of join().


## Example Application - $N$-Body Problem

- Many (?) problems involve computing all interactions between pairs of $N$ bodies - the " $N$-body problem". (Part of our molecular dynamics example fits this model.)
- Straightforward parallelization uses Task Parallelism. An alternate approach,


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 though, is based on the idea that a cluster of bodies far away can be treated as a single body (with mass the sum of the masses of the individual bodies, and position at the center of mass of the cluster). This leads to a divide-and-conquer approach ...
## $N$-Body Problem — Barnes-Hut Algorithm

- Idea of algorithm is to build a tree ("oct-tree") by repeatedly subdividing the whole space (splitting in half first in $x$ dimension, then $y$, then $z$, then $x$ again), discarding subdivisions with no bodies, until you get to one body per subdivision.

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- Pseudocode for algorithm then looks like this:
loop over time steps
build_octtree();
compute_mass_and_center_of_gravity();
compute_forces();
update_pos_and_velocity();
end loop
with computation of mass and center of gravity, and then forces, performed using the tree and a divide-and-conquer strategy.
$N$-Body Problem — Barnes-Hut Algorithm, Continued
- All but the last step and could be parallelized using Divide and Conquer. Load balance might be poor, but that can be corrected by splitting in a way that gives roughly equal numbers of particles in subdivisions.
- Last step could be parallelized with Task Parallelism.


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## Example Application - Prefix Sum

- Problem here is to compute, for each element $i$ of a list, the sum of that element and all elements to the left. Sounds purely sequential, right? but there is a clever Recursive Data solution ... (See book, pp. 101-102.)


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