# CSCI 4320 (Principles of Operating Systems), Fall 2006 

## Homework 3

Assigned: October 28, 2006.
Due: November 6, 2006, at 5pm.
Credit: 70 points.

## 1 Reading

Be sure you have read chapters 3 and 4.

## 2 Problems

Answer the following questions. You may write out your answers by hand or using a word processor or other program, but please submit hard copy, either in class or in my mailbox in the department office.

1. (5 points) Suppose you are designing an electronic funds transfer system, in which there will be many identical processes that work as follows: Each process accepts as input an amount of money to transfer, the account to be credited, and the account to be debited. It then locks both accounts (one at a time), transfers the money, and releases the locks when done. Many of these processes could be running at the same time. Clearly a design goal for this system is that two transfers that affect the same account should not take place at the same time, since that might lead to race conditions. However, no problems should arise from doing a transfer from, say, account $A$ to account $B$ at the same time as a transfer from account $C$ to account $D$, so another design goal is for this to be possible. The available locking mechanism is fairly primitive: It acquires locks one at a time, and there is no provision for testing a lock to find out whether it is available (you must simply attempt to acquire it, and wait if it's not available). A friend proposes a simple scheme for locking the accounts: First lock the account to be credited; then lock the account to be debited. Can this scheme lead to deadlock? If you think it cannot, briefly explain why not. If you think it can, first give an example of a possible deadlock situation, and then design a scheme that avoids deadlocks, meets the stated design goals, and uses only the locking mechanism just described.
2. ( 5 points) Consider a computer system with 10,000 bytes of memory whose MMU uses the simple base register / limit register scheme described in chapter 1 of the textbook (pages 2627 ), and suppose memory is currently allocated as follows:

- Locations 0-1999 are reserved for use by the operating system.
- Process $A$ occupies locations 4000-5999.
- Process $B$ occupies locations 6000-8999.
- Other locations are free.

Answer the following questions about this system.
(a) What value would need to be loaded into the base register if we performed a context switch to restart process $A$ ?
(b) What memory locations would correspond to the following virtual (program) addresses in process $A$ ?

- 100
- 4000

3. (5 points) Answer question 9 on p. 264 of the textbook. Tanenbaum says, in one of the questions at the end of the chapter, that although the 8086 processor provided no support for virtual memory, there were companies that sold computer systems that used an unmodified 8086 processor and did paging. How do you think they managed this? (Hint: Think about the logical location of the MMU.)
4. (5 points) Now consider a computer system using paging to manage memory; suppose it has $64 \mathrm{~K}\left(2^{16}\right)$ bytes of memory and a page size of 4 K bytes, and suppose the page table for some process (call it process $A$ ) looks like the following.

| Page number | Present/absent bit | Page frame number |
| ---: | ---: | ---: |
| 0 | 1 | 4 |
| 1 | 1 | 5 |
| 2 | 1 | 2 |
| 3 | 0 | $?$ |
| 4 | 0 | $?$ |
| 5 | 1 | 7 |
| 6 | 0 | $?$ |
| $\ldots$ | 0 | $?$ |
| 15 | 0 | $?$ |

Answer the following questions about this system.
(a) How many bits are required to represent a physical address (memory location) on this system? If each process has a maximum address space of 64 K bytes, how many bits are required to represent a virtual (program) address?
(b) What memory locations would correspond to the following virtual (program) addresses for process $A$ ? (Here, the addresses will be given in hexadecimal, i.e., base 16, to make the needed calculations simpler. Your answers should also be in hexadecimal. Notice that if you find yourself converting between decimal and hexadecimal, you are doing the problem the hard way. Stop and think whether there is an easier way.)

- 0x1420
- 0x2ff0
- 0x4008
- 0x0010
(c) If we want to guarantee that this system could support 16 concurrent processes and give each an address space of 64 K bytes, how much disk space would be required for storing out-of-memory pages? Justify your answer. (If your answer depends on making additional assumptions, state what they are - e.g., you might assume that the operating system will always use the first page frame of memory and will never be paged out.)

5. (10 points) Now consider a much bigger computer system, one in which addresses (both physical and virtual) are 32 bits and the system has $2^{32}$ bytes of memory. (You can express your answers in terms of powers of 2 , if that is convenient.) Answer the following questions about this system.
(a) What is the maximum size in bytes of a process's address space on this system?
(b) Is there a logical limit to how much main memory this system can make use of? That is, could we buy and install as much more memory as we like, assuming no hardware constraints? (Assume that the sizes of physical and virtual addresses don't change.)
(c) If page size is $4 \mathrm{~K}\left(2^{12}\right)$ and each page table entry consists of a page frame number and four additional bits (present/absent, referenced, modified, and read-only), how much space is required for each process's page table? (You should express the size of each page table entry in bytes, not bits, assuming 8 bits per byte and rounding up if necessary.)
(d) Suppose instead the system uses a single inverted page table (as described in chapter 4, pages $213-214$ ), in which each entry consists of a page number, a process ID, and four additional bits (free/in-use, referenced, modified, and read-only), and at most 64 processes are allowed. How much space is needed for this inverted page table? (You should express the size of each page table entry in bytes, not bits, assuming 8 bits per byte and rounding up if necessary.) How does this compare to the amount of space needed for 64 regular page tables?
6. (10 points) Consider a small computer system with only four page frames and address spaces consisting of eight pages. Suppose we start out with all page frames empty (pure demand paging) and run a program that references pages in the following order:

$$
0,1,7,2,3,2,7,1,0,3
$$

(That is, its first reference to memory is in page number 0 , its second reference to memory is in page number 1, etc.) Compute the number of page faults that occur during execution of this program if FIFO page replacement is used, and again if LRU page replacement is used. (Assume it is possible to implement LRU perfectly, so the page that is replaced really is the one least recently used.)
7. (5 points) Consider another small computer system with only four page frames. Suppose you have implemented the aging algorithm for page replacement, using 4-bit counters and updating the counters after every clock tick, and suppose the $R$ bits for the four pages are as follows after the first four clock ticks.

| Time | $R$ bit (page 0) | $R$ bit (page 1) | $R$ bit (page 2) | $R$ bit (page 3) |
| ---: | ---: | ---: | ---: | ---: |
| after tick 1 | 0 | 1 | 1 | 1 |
| after tick 2 | 1 | 0 | 1 | 1 |
| after tick 3 | 1 | 0 | 1 | 0 |
| after tick 4 | 1 | 1 | 0 | 1 |

What are the values of the counters (in binary) for all pages after these four clock ticks? If a page needed to be removed at that point, which page would be chosen for removal?
8. (5 points) The operating system designers at Acme Computer Company have been asked to think of a way of reducing the amount of disk space needed for paging. One person
proposes never saving pages that only contain program code, but simply paging them in directly from the file containing the executable. Will this work always, never, or sometimes? If "sometimes", when will it work and when will it not? (Hint: Search your recollections of CSCI 2321 - or another source - for a definition of "self-modifying code".)
9. (5 points) A computer at Acme Company used as a compute server (i.e., to run batch jobs) is observed to be running slowly (turnaround times longer than expected). The system uses demand paging, and there is a separate disk used exclusively for paging. The sysadmins are puzzled by the poor performance, so they decide to monitor the system. It is discovered that the CPU is in use about $20 \%$ of the time, the paging disk is in use about $98 \%$ of the time, and other disks are in use about $5 \%$ of the time. For each of the following, say whether it would be likely to increase CPU utilization and why.
(a) Installing a faster CPU.
(b) Installing a larger paging disk.
(c) Increasing the number of processes (degree of multiprogramming).
(d) Decreasing the number of processes (degree of multiprogramming).
(e) Installing more main memory.
(f) Installing a faster paging disk.
10. (5 points) How long it takes to access all elements of a large data structure can depend on whether they're accessed in contiguous order (i.e., one after another in the order in which they're stored in memory), or in some other order. The classic example is a 2D array, in which performance of nested loops such as

```
for (int r = 0; r < ROWS; ++r)
    for (int c = 0; c < COLS; ++c)
        array[r][c] = foo(r,c);
```

can change drastically for a large array if the order of the loops is reversed. Give an explanation for this phenomenon based on what you have learned from our discussion of memory management. For extra credit, give another explanation that might also be true for a computer such as one of our lab machines.

## 3 Programming Problems

Do the following programming problems. You will end up with at least one code file per problem. Submit your program source (and any other needed files) by sending mail to bmassing@cs. trinity.edu, with each file as an attachment. Please use a subject line that mentions the course number and the assignment (e.g., "csci 4320 homework 3"). You can develop your programs on any system that provides the needed functionality, but I will test them on one of the department's Fedora Core 5 Linux machines, so you should probably make sure they work in that environment before turning them in.

1. (10 points) Write a program or programs to demonstrate the phenomenon described in problem 10. Turn in your program(s) and output showing differences in execution time. (It's probably simplest to just put this output in a text file and send that together with your source
code file(s).) I'd prefer programs in C, C++, or Java, but anything that can be compiled and executed on one of the FC5 lab machines is fine (as long as you tell me how to compile and execute what you turn in, if it's not C/C++ or Java). You don't have to develop and run your programs on one of the FC5 lab machines, but if you don't, (1) tell me what system you used instead, and (2) be sure your programs at least compile and run on one of the lab machines, even if they don't necessarily give the same timing results as on the system you used.

Possibly helpful hints:

- An easy way to measure how long program mypgm takes on a Linux system is to run it by typing time mypgm. Another way is to run it with /usr/bin/time mypgm. (This gives more/different information - try it.) If you'd rather put something in the program itself to collect and print timing information, for $\mathrm{C} / \mathrm{C}++$ programs you could use the function in timer. ${ }^{1}$ to obtain starting and ending times for the section of the code you want to time, or for Java programs you could use System.currentTimeMillis.
- Your program doesn't have to use a 2D array (you might be able to think of some other data structure that produces the same result). If you do use a 2 D array, though, keep in mind the following:
- To the best of my knowledge, C and C++ allocate local variables on the stack, which may be limited in size. Dynamically allocated variables (i.e., those allocated with malloc or new) aren't subject to this limit.
- Dynamic allocation of 2D arrays in C is full of pitfalls. It may be easier to just allocate a 1D array and fake accessing it as a 2D array (e.g., the element in $x[i][j]$, if $x$ is a $2 D$ array, is at offset $i * n c o l s+j)$.

[^0]
[^0]:    ${ }^{1}$ http://www.cs.trinity.edu/~ bmassing/Classes/CS4320_2006fall/Homeworks/HW03/Problems/timer.h

