

# Experimental Design

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# Opening Discussion

- Minute Essay comments
  - Are virtual computers/emulators considered simulations?

# 2<sup>k</sup> Factorial Designs

- Imagine a system with  $k$  factors. We want to vary each one to see how much the system depends on it.
- We can vary them each independently for sensitivity analysis. This gives  $2^k$  simulations. Requires lots of simulations and doesn't explore interactions.
- Look at average difference between all runs where a value is low vs. high.

# Interactions

- We can also look at two factor differences. We want the average for one factor at plus and minus only in cases where another factor was at plus or minus.

# Covering Parameter Space

- Sometimes you want more than just the + and – options for a value.
- In physical simulation there are often ranges of values that are physically significant and you want to check a range of those.
- This can only be done nicely for small dimensional parameter spaces.

# $2^{k-p}$ Fractional Factorial

- The “standard”  $2^k$  factorial design method can often require far too many simulations.
- There are approaches where you don't cover the space quite as completely for large  $k$  situations yet still get most of the benefit.
- This section of the text has a lot of details in it on how you would design a test suite that doesn't fully investigate certain parameters. It does leave you with some ambiguity though.

# Metamodels

- The earlier experimental design plans mainly aimed to allow you to see how a system responds relative to changes in certain variables. They also allowed exploration of mutual changes.
- Often you would like to be able to predict the response of a system based on a few of the factors.
- This basically uses linear regression to fit responses.

# Building Models

- The type of model that you can build will depend a lot on the number of different values you try for each factor.
- With only two values, the model has to have no more than two parameters and will likely be linear. Larger numbers of data points can give you higher order fits.
- You want fits, not just interpolating of data.

# Response Surfaces

- Another way to model data is to build a response surface.
- This is basically like what I showed you for my ring simulations.
- You vary 2 factors through a few values to form a surface of responses.
- If you had the right visualization software/hardware you might try to build a response space, but it can be harder to interpret.

# Simulation Based Optimization

- Optimization is a field unto itself.
- The challenge with simulation is that evaluating new points in the parameter space can be costly.
- Unconstrained optimization basically uses Newton's method in a higher dimensional space. Derivatives typically taken numerically.
- Constrained optimization places bounds on where the solution can be. Linear programming.

# Minute Essay

- Any questions?